

Linear inequalities

A LEVEL LINKS

Scheme of work: 1d. Inequalities – linear and quadratic (including graphical solutions)

Key points

- Solving linear inequalities uses similar methods to those for solving linear equations.
- When you multiply or divide an inequality by a negative number you need to reverse the inequality sign, e.g. < becomes >.

Examples

Example 1 Solve $-8 \le 4x < 16$

| $-8 \le 4x < 16$ | Divide all three terms by 4. |
|------------------|------------------------------|
| $-2 \le x < 4$ | |

Example 2 Solve $4 \le 5x < 10$

| $4 \le 5x < 10$ | Divide all three terms by 5. |
|-------------------------|------------------------------|
| $\frac{4}{5} \le x < 2$ | |

Example 3 Solve 2x - 5 < 7

| 2x - 5 < 7 | 1 Add 5 to both sides. |
|--------------|----------------------------------|
| 2x < 12 | 2 Divide both sides by 2. |
| <i>x</i> < 6 | |

Example 4 Solve $2 - 5x \ge -8$

| $ \begin{array}{c c} -5x \ge -10 \\ x \le 2 \end{array} $ 2 Diving Rem | otract 2 from both sides. ide both sides by -5. nember to reverse the inequality on dividing by a negative other. |
|--|---|
|--|---|

Example 5 Solve 4(x-2) > 3(9-x)

| 4(x-2) > 3(9-x) $4x-8 > 27-3x$ $7x-8 > 27$ $7x > 35$ $x > 5$ | Expand the brackets. Add 3x to both sides. Add 8 to both sides. Divide both sides by 7. |
|--|--|
|--|--|





Practice

Solve these inequalities.

a
$$4x > 16$$

b
$$5x - 7 \le 3$$

b
$$5x - 7 \le 3$$
 c $1 \ge 3x + 4$

d
$$5-2x < 12$$

$$\frac{x}{2} \ge 3$$

d
$$5-2x < 12$$
 e $\frac{x}{2} \ge 5$ **f** $8 < 3 - \frac{x}{3}$

Solve these inequalities.

a
$$\frac{x}{5} < -4$$

$$\mathbf{b} \qquad 10 \ge 2x + 3$$

b
$$10 \ge 2x + 3$$
 c $7 - 3x > -5$

3 Solve

a
$$2 - 4x \ge 18$$

a
$$2-4x \ge 18$$
 b $3 \le 7x + 10 < 45$ **c** $6-2x \ge 4$ **d** $4x + 17 < 2 - x$ **e** $4-5x < -3x$ **f** $-4x \ge 24$

c
$$6 - 2x > 4$$

d
$$4x + 17 < 2 - x$$

e
$$4-5x < -3x$$

$$f -4x \ge 24$$

4 Solve these inequalities.

a
$$3t + 1 < t + 6$$

b
$$2(3n-1) \ge n+5$$

5 Solve.

a
$$3(2-x) > 2(4-x) + 4$$
 b $5(4-x) > 3(5-x) + 2$

b
$$5(4-x) > 3(5-x) + 2$$

Extend

Find the set of values of x for which 2x + 1 > 11 and 4x - 2 > 16 - 2x.





Answers

a x > 4

b $x \le 2$ **c** $x \le -1$

d $x > -\frac{7}{2}$

e $x \ge 10$

f x < -15

2 **a** x < -20

b $x \le 3.5$

c x < 4

3 **a** $x \le -4$

b $-1 \le x < 5$

c $x \le 1$

d x < -3

x > 2

 $\mathbf{f} \qquad x \leq -6$

4 **a** $t < \frac{5}{2}$

 $\mathbf{b} \qquad n \ge \frac{7}{5}$

5 **a** x < -6

b $x < \frac{3}{2}$

6 x > 5 (which also satisfies x > 3)